

Directions: Calculators are not allowed.

1) If the equation  $y = \left(\frac{1}{8}\right)^x$  is graphed, which of the following values of  $x$  would produce a point closest to the  $x$ -axis? *decay → largest*

A)  $\frac{1}{8} = .125$

B)  $\frac{1}{2} = .5$

C)  $\frac{4}{3} = 1.\overline{33}$

D)  $\frac{5}{2} = 2.5$

2) If the equation  $y = 9^x$  is graphed, which of the following values of  $x$  would produce a point closest to the  $x$ -axis? *growth → smallest*

A)  $\frac{1}{7}$

B)  $\frac{2}{3}$

C)  $\frac{5}{4}$

D)  $\frac{9}{4}$

3) Express each equation in exponential form.

A)  $\log_8 \frac{1}{2} = x$

$8^x = \frac{1}{2}$

B)  $\log_5 125 = 3$

$5^3 = 125$

4) Express each equation in logarithmic form.

A)  $8^2 = 64$   $\log_8 64 = 2$

B)  $c^y = 5$   $\log_c 5 = y$

C)  $7^a = y$   $\log_7 y = a$

5) Expand each logarithm as much as possible.

A)  $\log_3 \sqrt[3]{xy}$

B)  $\log(8a^5)$

C)  $\ln \frac{6b^2}{x}$

D)  $\log_3 \frac{x^4}{a^3 b^2}$

6) Condense each logarithm as much as possible.

A)  $5 \log n + \log 8$

$\log 8n^5$

B)  $\log y - 3 \log b$

$\log \frac{y}{b^3}$

C)  $\log_6 24 - 3 \log_6 2 + \log_6 c$

$\log_6 3c$

D)  $2 \ln k + \ln y - 4 \ln a$

$\ln \frac{k^2 y}{a^4}$

7) Evaluate each of the following logarithms.

A)  $\log_3 27$

3

B)  $\log_5 \frac{1}{25}$

-2

C)  $\ln(e^6)$

6

D)  $\ln(e^{-2})$

-2

E)  $\log_4 1$

0

8) Express each logarithm as a quotient of common logarithms.

A)  $\log_3 90$

$\frac{\log 90}{\log 3}$

B)  $\log_b 25$

$\frac{\log 25}{\log b}$

9) Simplify each product as much as possible. Do not leave negative exponents in your answer.

A)  $\frac{6e^x}{5e^{-3x}} \cdot \frac{e^{5x}}{12}$

$\frac{e^{9x}}{10}$

B)  $\frac{2e^{-4x}}{e^{2x}} \cdot \frac{e^{-x}}{8}$

$\frac{1}{4e^{7x}}$

10) If  $\log 2 \approx 0.301$  and  $\log 5 \approx 0.699$ , what is the approximate value of each logarithm.

A)  $\log 10$

1

B)  $\log_5^2$

-0.398

C)  $\log 20$

1.301

11) If  $\log 3 = x$  and  $\log 6 = n$ , express each logarithm in terms of  $x$  and/or  $n$ .

- A)  $\log 2$   $n-x$       B)  $\log 18$   $n+x$       C)  $\log 12$   $2n-x$

12) Solve each equation for  $x$ .

A)  $7^x = 20$  (Express answer as a quotient of common logarithms.)

$\frac{\log 20}{\log 7}$

B)  $4(2^x) - 1 = 23$  (Express answer as a quotient of common logarithms.)

$\frac{\log 6}{\log 2}$

C)  $\frac{1}{3}e^x = 10$  (Express answer as a natural logarithm.)

$\ln 30$

D)  $\log_5(x-1) = 2$  (Express answer as a number.)

26

E)  $\log_2(3x+4) = 3$  (Express answer as a number.)

$\frac{4}{3}$

F)  $\log_x \frac{1}{100} = -2$  (Express answer as a number.)

10

G)  $\log_2 x = -3$  (Express answer as a number.)

$\frac{1}{8}$

H)  $\log_6 7 + \log_6 x = 2$  (Express answer as a number.)

$\frac{36}{7}$

I)  $\log 4 + \log x = \log 6 + \log 2$  (Express answer as a number.)

3

J)  $\log_2 x - \log_2 5 = 1$  (Express answer as a number.)

10

13) Which is the first **incorrect** step in each expansion?

A) Step 1:  $\log_4 \frac{4}{16} = \log_4 4 - \log_4 16$  ✓

Step 2:  $= 1 - \log_4 16$  ✓

Step 3:  $= 1 - 4$  ← No.  $\log_4 16 = 2$  not  $4$

Step 4:  $= -3$

Think  $4^x = 16$

B) Step 1:  $\log \frac{7a^3}{5b^2} = \log 7a^3 - 5b^2$  ← No. should be

Step 2:  $= \log 7 + \log a^3 - \log 5b^2$

Step 3:  $= \log 7 + \log a^3 - \log 5 + \log b^2$

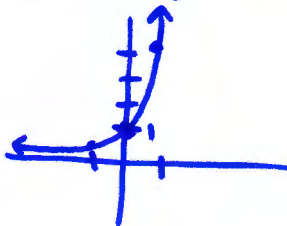
Step 4:  $= \log 7 + 3 \log a - \log 5 + 2 \log b$

$\log 7a^3 - \log 5b^2$

14) Sketch a graph of each exponential function. Your graph must have the correct key point, approach the correct asymptote, and have the correct curvature.

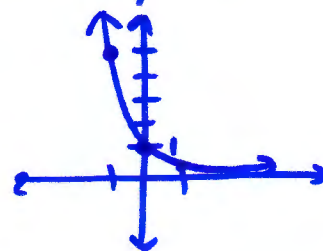
A)  $f(x) = 4^x$  → growth

x	y
-1	1/4
0	1
1	4



B)  $y = (\frac{1}{5})^x$  → decay

x	y
-1	5
0	1
1	1/5



$$\boxed{3} \quad \text{A) } 8^x = \frac{1}{2} \quad \text{B) } 5^3 = 125$$

$$\boxed{4} \quad \text{A) } \log_8 64 = 2 \quad \text{B) } \log_c 5 = y \quad \text{C) } \log_7 y = a$$

$$\boxed{5} \quad \text{A) } \log \sqrt[3]{xy} = \log (xy)^{\frac{1}{3}} \\ = \frac{1}{3} \log xy = \frac{1}{3} \log x + \frac{1}{3} \log y$$
$$\text{B) } \log (8a^5) = \log 8 + \log a^5 \\ = \log 8 + 5 \log a$$

$$\text{C) } \ln \frac{6b^2}{x} = \ln 6b^2 - \ln x \\ = \ln 6 + \ln b^2 - \ln x \\ = \ln 6 + 2 \ln b - \ln x$$

$$\text{D) } \log_3 \frac{x^4}{a^3 b^2} = \log_3 x^4 - \log_3 a^3 b^2 \\ = \log_3 x^4 - \log_3 a^3 - \log_3 b^2 \\ = 4 \log_3 x - 3 \log_3 a - 2 \log_3 b$$

$$\boxed{6} \quad \text{A) } \overrightarrow{5 \log n} + \log 8 \\ = \log n^5 + \log 8 \\ = \log 8n^5$$

$$\text{B) } \log y - 3 \log b \\ = \log y - \log b^3 \\ = \log \frac{y}{b^3}$$

$$\text{C) } \log_6 24 - \overrightarrow{3 \log_6 2} + \log_6 c \\ = \log_6 24 - \log_6 2^3 + \log_6 c \\ = \log_6 \frac{24}{8} + \log_6 c \\ = \log_6 3 + \log_6 c \\ = \log_6 3c$$

$$\text{D) } \overrightarrow{2 \ln k} + \ln y - \overrightarrow{4 \ln a} \\ = \ln k^2 + \ln y - \ln a^4 \\ = \ln k^2 y - \ln a^4 \\ = \ln \frac{k^2 y}{a^4}$$

$$\boxed{7} \quad \text{A) } \log_3 27 = 3$$

$$\text{D) } \ln(e^{-2}) = -2 \ln e = -2$$

$$\text{B) } \log_5 \frac{1}{25} = -2$$

$$\text{E) } \log_4 1 = 0$$

$$\text{C) } \ln(e^6) = 6 \ln e = 6$$

$$\boxed{8} \quad \text{A) } \log_3 90 = \frac{\log 90}{\log 3} \quad \text{B) } \log_b 25 = \frac{\log 25}{\log b}$$

$$\boxed{9} \quad \text{A) } \frac{6e^x}{5e^{-3x}} \cdot \frac{e^{5x}}{12} = \frac{6e^{6x}}{60e^{-3x}} \uparrow = \frac{6e^{9x}}{60} = \frac{e^{9x}}{10}$$

$$\text{B) } \frac{2e^{-4x}}{e^{2x}} \cdot \frac{e^{-x}}{8} = \frac{2e^{-5x}}{8e^{2x}} \downarrow = \frac{2}{8e^{7x}} = \frac{1}{4e^{7x}}$$

$$\rightarrow \log 2 \approx .301 \quad \log 5 \approx .699$$

$$\boxed{10} \quad \text{A) } \log 10 = \log 2 \cdot 5 = \log 2 + \log 5 = .301 + .699 = \boxed{1}$$

$$\text{B) } \log \frac{2}{5} = \log 2 - \log 5 = .301 - .699 = \boxed{-0.398}$$

$$\text{C) } \log 20 = \log 2 \cdot 2 \cdot 5 = \log 2 + \log 2 + \log 5 =$$

$$= .301 + .301 + .699 = \boxed{1.301}$$

$$\boxed{11} \quad \log 3 = x \quad \log 6 = n$$

$$\text{A) } \log 2 = \log \frac{6}{3} = \log 6 - \log 3 = \boxed{n-x}$$

$$\text{B) } \log 18 = \log 3 \cdot 6 = \log 3 + \log 6 = \boxed{x+n} \quad \text{or} \quad \boxed{n+x}$$

$$\text{C) } \log 12 = \log \frac{6 \cdot 6}{3} = \log 6 + \log 6 - \log 3$$

$$n + n - x$$

$$\boxed{2n-x}$$

$$\boxed{12} \quad A) 7^x = 20$$

$$\log_7 20 = x$$

$$\frac{\log 20}{\log 7}$$

$$B) 4(2^x) - 1 = 23$$

$$\frac{4(2^x)}{4} = \frac{24}{4}$$

$$2^x = 6$$

$$x = \log_2 6$$

$$x = \frac{\log 6}{\log 2}$$

$$C) \frac{1}{3} e^x = 10 \cdot 3$$

$$e^x = 30$$

$$\log_e 30 = x$$

$$\ln 30 = x$$

$$x = \ln 30$$

$$D) \log_5(x-1) = 2$$

$$5^2 = x-1$$

$$25 = x - 1$$

$$\frac{+1}{26}$$

$$x = 26$$

$$E) \log_2(3x+4) = 3$$

$$2^3 = 3x+4$$

$$8 = 3x+4$$

$$\frac{-4}{4} = \frac{-4}{3}$$

$$\frac{4}{3} = \frac{3x}{3}$$

$$x = \frac{4}{3}$$

$$F) \log_x^{-2} = \frac{1}{100}$$

$$x^{-2} = \frac{1}{100}$$

$$\frac{1}{x^2} = \frac{1}{100}$$

$$\hookrightarrow x = 10$$

$$G) \log_2 x = -3$$

$$2^{-3} = x$$

$$\frac{1}{2^3} = x$$

$$\hookrightarrow x = \frac{1}{8}$$

$$H) \log_6 7 + \log_6 x = 2$$

$$\log_6 7x = 2$$

$$6^2 = 7x$$

$$\frac{36}{7} = \frac{7x}{7}$$

$$x = \frac{36}{7}$$

$$I) \log 4 + \log x = \log 6 + \log 2$$

$$\log 4x = \log 12$$

$$\frac{4x}{4} = \frac{12}{4}$$

$$\hookrightarrow x = 3$$

$$J) \log_2 x - \log_2 5 = 1$$

$$\log_2 \frac{x}{5} = 1$$

$$\rightarrow 2^1 = \frac{x}{5}$$

$$2 = \frac{x}{5}$$

$$5 \cdot 2 = \frac{x}{5} \cdot 5$$

$$10 = x$$